# Pattern mining in personal demographic trajectories

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Ignatov et al. Pattern mining in personal demographic trajectories

- First job (job)
- The highest education degree is obtained (education)
- Leaving parents' home (separation)
- First partner (partner)
- First marriage (marriage)
- First child birth (children)
- Break-up (parting)
- ... (divorce)

Generation and Gender Survey (GGS): three waves panel data for 11 generations of Russian citizens starting from 30s

# Binary classification 1545 men 3312 women

#### Examples of sequential patterns

- $\langle \{education, separation\}, \{work\}, \{marriage\}, \{children\} \rangle (m)$
- $\langle \{work\}, \{marriage\}, \{children\} \{education\} \rangle (f)$
- $\langle \{partner\}, \{marriage, separation\}, \{children\} \rangle (f)$

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- $s = \langle s_1, ..., s_k \rangle$  is the subsequence of  $s' = \langle s'_1, ..., s'_k \rangle$   $(s \leq s')$  if  $k \leq k'$  and there exist  $1 \leq r_1 < r_2 < ... < r_k \leq k'$  such  $s_j = s'_{r_j}$  for all  $1 \leq j \leq k$ .
- support(s, D) is the support of a sequence s in D, i.e. the number of sequences in D such that s is their subsequence.

$$support(s, D) = |\{s'|s' \in D, s \leq s'\}|$$

s is a frequent closed sequence (sequential pattern) if there is no s' such that s ≺ s' and

$$support(s, D) = support(s', D)$$

Let D be a set of sequences:

Таблица:	Dataset	D.
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<i>s</i> <sub>1</sub>	${a, b, c}{a, b}{b}$
<i>s</i> <sub>2</sub>	$\{a\}\{a,c\}\{a\}$
<i>s</i> 3	$\{a,b\}\{b,c\}$

- $I = \{a, b, c\}$  is the set of all items (atomic events)
- $\langle \{a,b\}\{b\} \rangle$  belongs to  $s_1$  and  $s_3$  but it is missing in  $s_2$
- $support_D(\langle \{a, b\} \{b\} \rangle) = 2$
- $\{\langle \{a\}\rangle, \langle \{c\}\rangle, \langle \{a\}\{c\}\rangle, \langle \{a,b\}\{b\}\rangle, \langle \{a,c\}\{a\}\rangle\}$  is the set of closed sequences.

#### CAEP: Classification by Aggregating Emerging Patterns G. Dong et al., 1999

#### Growth Rate

$$growth\_rate_{D'\to D''}(X) = \begin{cases} \frac{supp_{D''}(X)}{supp_{D'}(X)} \text{ if } supp_{D'}(X) \neq 0\\ 0 \text{ if } supp_{D''}(X) = supp(X) = 0\\ \infty \text{ if } supp_{D''}(X) \neq 0 \text{ and } supp_{D'}(X) = 0 \end{cases}$$

#### Class score

$$score(s, C) = \sum_{e \subseteq s, e \in E(c)} \frac{growth\_rate_{C}(e)}{growth\_rate_{C}(e) + 1} \cdot supp_{c}(e)$$

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# CAEP: Classification by Aggregating Emerging Patterns

#### Score normalization

$$normal\_score(s, C) = \frac{score(s, C)}{median(\{growth\_rate_{C}(e_{i})\})}$$

#### Classification rule

$$class(s) = \begin{cases} C_1, if normal\_score(s, C_1) > normal\_score(s, C_2) \\ C_2, if normal\_score(s, C_1) < normal\_score(s, C_2) \\ undetermined if normal\_score(s, C_1) = normal\_score(s, C_2) \end{cases}$$

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- $s = \langle s_1, ..., s_k \rangle$  is a gapless prefix-based subsequence of  $s' = \langle s'_1, ..., s'_k \rangle$  (s\* = s') if  $k \le k'$  and  $\forall i \in k' : s_i = s'_i$ .
- Support of gapless prefix-based sequences Let *T* be a set of sequences.

$$support(s, T) = \frac{|\{s'|s' \in T, s* = s'\}|}{|T|}$$

- Let 0 < minSup ≤ 1 be a minimal support parameter and D is a set of sequences then searching for prefix-based gapless sequential patterns is the task of enumeration of all prefix-based gapless sequences s such that support(s, D) ≥ minSup. Every sequence s with support(s, D) ≥ minSup is called a prefix-based gapless sequential pattern.
- Prefix-based gapless sequential pattern (PGSP) p is called closed if there is no PGSP d of greater of equal support such that d = p\*.

# Gapless sequential patterns

#### Example

Таблица: D is a set of sequences.

<i>s</i> <sub>1</sub>	$\{a\}\{b\}\{d\}$
<i>s</i> <sub>2</sub>	a $b$ $c$
<i>s</i> 3	$\{a,b\}\{b,c\}$

 $s = \langle \{a\}\{b\} \rangle$ 

- $I = \{a, b, c\}$  is the set of all items (atomic events)
- $s_1 = s_*; s_2 = s_*$
- $s_3 \neq s*$
- $Supp_D(s) = \frac{2}{3}$
- $\langle \{a\}\{b\}\rangle$  is closed,  $\langle \{a\}\rangle$  is not closed.

- $(S, (D, \sqcap), \delta)$  is a pattern structure
- S is a set of objects, D is a set of their their possible descriptions
- $\delta(g)$  is the description of g from S
- Galois connection is given by  $\diamond$  operator as follows:

$$A^\diamond := \prod_{g \in A} \delta(g)$$
 for  $A \subseteq S$ 

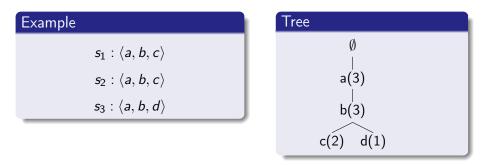
$$d^\diamond := \{s \in S | d \sqsubseteq \delta(g)\}$$
 for  $d \in D$ 

 For two sequences □ may result in their largest common prefix subsequence

# A pair (A, d) is called a **pattern concept** of a pattern structure $(S, (D, \Box), \delta)$ if

- $\bullet A \subseteq S$
- $\mathbf{2} \ d \in D$
- $A^\diamond = d$
- $d^\diamond = A$

# Pattern Structures



Pattern concepts (PCs)

$$(\{s_1, s_2, s_3\}, \langle a, b \rangle); (\{s_1, s_2\}, \langle a, b, c \rangle)$$
$$(\{s_3\}, \langle a, b, d \rangle)$$
$$(\{s_1\}, \langle a, b, c \rangle) \text{ is not a PC}$$

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#### Positive, negative and undetermined pattern structures

$$\mathbb{K}_{\oplus} = (S_{\oplus}, (D, \sqcap), \delta_{\oplus})$$
  
 $\mathbb{K}_{\ominus} = (S_{\ominus}, (D, \sqcap), \delta_{\ominus})$ 

There is a pattern structure of undetermined examples:

$$\mathbb{K}_{\tau} = (S_{\tau}, (D, \sqcap), \delta_{\tau})$$

#### Hypothesis

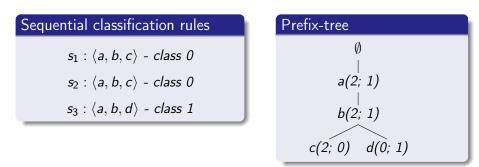
A **hypothesis** is a pattern intent that belongs to examples from a fixed class only

A pattern intent h is a positive hypothesis (dually for negative hypotheses) if

$$orall s\in \mathcal{S}_{\ominus}(s\in \mathcal{S}_{\oplus}):h
ot\equiv s^{\ominus}(h
ot\equiv s^{\oplus})$$

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#### Hypotheses

 $\langle \{a\}, \{b\}, \{c\} \rangle$  is a hypothesis of class 0  $\langle \{a\}, \{b\}, \{d\} \rangle$  is a hypothesis of class 1

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$$class(g_{\tau}) = \begin{cases} positive \text{ if } \exists h_{\oplus}, h_{\oplus} \sqsubseteq \delta(g_{\tau}) \text{ and } \nexists h_{\ominus}, h_{\ominus} \sqsubseteq \delta(g_{\tau}) \\ negative \text{ if } \nexists h_{\oplus}, h_{\oplus} \sqsubseteq \delta(g_{\tau}) \text{ and } \exists h_{\ominus}, h_{\ominus} \sqsubseteq \delta(g_{\tau}) \\ undetermined \text{ if } \exists h_{\oplus}, h_{\oplus} \sqsubseteq \delta(g_{\tau}) \text{ and } \exists h_{\ominus}, h_{\ominus} \sqsubseteq \delta(g_{\tau}) \\ undetermined \text{ if } \nexists h_{\oplus}, h_{\oplus} \sqsubseteq \delta(g_{\tau}) \text{ and } \nexists h_{\ominus}, h_{\ominus} \sqsubseteq \delta(g_{\tau}) \end{cases}$$

### Growth Rate

$${\it GrowthRate}(s,\mathbb{K}_\oplus,\mathbb{K}_\ominus)=rac{{\it Sup}_{\mathbb{K}_\oplus}(s)}{{\it Sup}_{\mathbb{K}_\ominus}(s)}$$

#### Emerging patterns

A pattern is called **emerging pattern** if its growth rate is greater than or equal to  $\Theta_{\textit{min}}$ 

$${\it GrowthRate}(g, \mathbb{K}_\oplus, \mathbb{K}_\ominus) > \Theta_{\it min}$$

#### s is a new object

$$normal\_score_{\oplus}(s) = \frac{\sum_{p \in P_{\oplus}: p \sqsubseteq s} GrowthRate(p, \mathbb{K}_{\oplus}, \mathbb{K}_{\ominus})}{median(GrowthRate(P_{\oplus}))}$$
$$normal\_score_{\ominus}(s) = \frac{\sum_{p \in P_{\ominus}: p \sqsubseteq s} GrowthRate(p, \mathbb{K}_{\ominus}, \mathbb{K}_{\oplus})}{median(GrowthRate(P_{\ominus}))}$$

### Classification via emerging patterns

$$class(s) = \begin{cases} positive \ if \ normal\_score_{\oplus}(s) > normal\_score_{\ominus}(s) \\ negative \ if \ normal\_score_{\oplus}(s) < normal\_score_{\ominus}(s) \\ undetermined \ if \ normal\_score_{\oplus}(s) = normal\_score_{\ominus}(s) \end{cases}$$

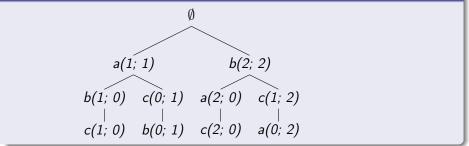
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- Build the prefix tree for the input sequences.
- Is For each tree node calculate its Growth Rate.
- Solution For every new sequence traverse the tree and compute the Score for each class.
- Compare the Score value for different classes and classify the new sequence.

#### Input sequences

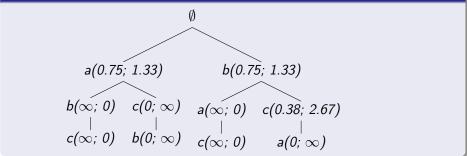
# $\begin{array}{l} class\_0: \{\langle \{a\}\{b\}\{c\}\rangle, \langle \{b\}\{a\}\{c\}\rangle, \langle \{b\}\{a\}\{c\}\rangle, \langle \{b\}\{c\}\rangle\} \\ class\_1: \{\langle \{a\}\{c\}\{b\}\rangle, \langle \{b\}\{c\}\{a\}\rangle, \langle \{b\}\{c\}\{a\}\rangle\} \end{array} \end{array}$

#### Prefix tree



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#### Counting Growth Rate



New sequence

 $\langle \{b\}; \{c\}; \{a\} \rangle -???$ 

 $Score_0 = 0$ 

$$Score_1 = 2.67 + \infty = \infty$$

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## Comparison of closed and non-closed patterns

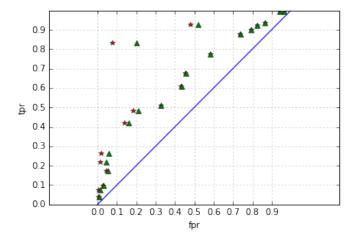
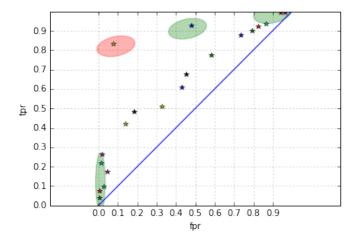


Рис.: TPR vs FPR for closed and non-closed patterns

## Experiments and results



Puc.: TPR-FPR for classification by gender via gapless prefix-based patterns

 $(\langle \{work, separation\}, \{marriage\}, \{children\}, \{education\}\rangle, [\infty, 0.006])$ 

 $(\langle \{separation, partner\}, \{marriage\}\rangle, [\infty, 0.006])$ 

 $(\langle \{work, separation\}, \{marriage\}, \{children\}\rangle, [\infty, 0.008])$ 

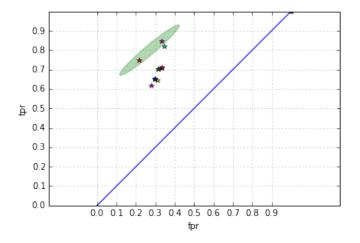
 $(\langle \{work, separation\}, \{marriage\} \rangle, [\infty, 0.009])$ 

 $(\langle \{education\}, \{marriage\}, \{work\}, \{children\}, \{separation\}\rangle, [10.6, 0.006])$ 

 $(\langle \{ education \}, \{ marriage \}, \{ work \}, \{ children \} \rangle, [12.7, 0.007] )$ 

 $(\langle \{educ\}, \{work\}, \{part\}, \{mar\}, \{sep\}, \{ch\}\rangle, [10.6, 0.006])$ 

## Experiments and results



Puc.: TPR-FPR for classification by generation via gapless prefix-based patterns

# Interesting patterns (Different Generations; Women)

#### Old women

$$(\langle \{work\}, \{separation\}\rangle, [1.85, 0.38])$$

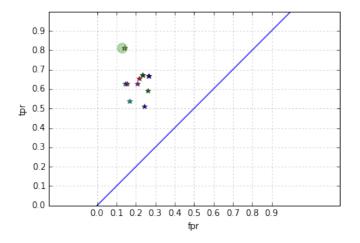
 $(\langle \{work\}, \{marriage, separation\} \rangle, [3.92, 0.08])$ 

#### Young women

 $(\langle \{ education \} \rangle, [1.84, 0.26])$  $(\langle \{ education \}, \{ work \} \rangle, [4.01, 0.1])$ 

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## Experiments and results



Puc.: TPR-FPR for classification by generation via gapless prefix-based patterns

#### Old men

 $(\langle \{ work \}, \{ marriage, separation \}, \{ education \} \rangle, [13.52, 0.025] ) \\ (\langle \{ work \}, \{ marriage \}, \{ separation \} \rangle, [22.87, 0.042] ) \\ (\langle \{ work \}, \{ marriage \}, \{ separation \}, \{ education \} \rangle, [\infty, 0.0208] )$ 

#### Young men

 $(\langle \{ education \}, \{ work \}, \{ separation \}, \{ marriage \}, \{ children \} \rangle, [10.58, 0.020] ) \\ (\langle \{ education \}, \{ work \}, \{ separation, partner \}, \{ marriage \} \rangle, [8.65, 0.016] ) \\ (\langle \{ education \}, \{ marriage, separation \} \rangle, [7.69, 0.015] )$ 

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- We have studied several pattern mining techniques for demographic sequences including pattern-based classification in particular.
- We have fitted existing approaches for sequence mining of a special type (gapless and prefix-based ones).
- The results for different demographic groups (classes) have been obtained and interpreted.
- In particular, a classifier based on emerging sequences and pattern structures has been proposed.

Thank you!

Questions?

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